

The College Board
Advanced Placement Examination
PHYSICS C
SECTION II

TABLE OF INFORMATION FOR 1998

CONSTANTS AND CONVERSION FACTORS		UNITS		PREFIXES																																		
1 unified atomic mass unit,	$1u = 1.66 \times 10^{-27} \text{ kg}$ $= 931 \text{ MeV}/c^2$	Name	Symbol	Factor	Prefix	Symbol																																
Proton mass,	$m_p = 1.67 \times 10^{-27} \text{ kg}$	meter	m	10^9	giga	G																																
Neutron mass,	$m_n = 1.67 \times 10^{-27} \text{ kg}$	kilogram	kg	10^6	mega	M																																
Electron mass,	$m_e = 9.11 \times 10^{-31} \text{ kg}$	second	s	10^3	kilo	k																																
Magnitude of the electron charge,	$e = 1.60 \times 10^{-19} \text{ C}$	ampere	A	10^{-2}	centi	c																																
Avogadro's number,	$N_0 = 6.02 \times 10^{23} \text{ mol}^{-1}$	kelvin	K	10^{-3}	milli	m																																
Universal gas constant,	$R = 8.31 \text{ J}/(\text{mol} \cdot \text{K})$	mole	mol	10^{-6}	micro	μ																																
Boltzmann's constant,	$k_B = 1.38 \times 10^{-23} \text{ J/K}$	hertz	Hz	10^{-9}	nano	n																																
Speed of light,	$c = 3.00 \times 10^8 \text{ m/s}$	newton	N	10^{-12}	pico	p																																
Planck's constant,	$h = 6.63 \times 10^{-34} \text{ J} \cdot \text{s}$ $= 4.14 \times 10^{-15} \text{ eV} \cdot \text{s}$	pascal	Pa	VALUES OF TRIGONOMETRIC FUNCTIONS FOR COMMON ANGLES <table border="1" style="margin: 0 auto; border-collapse: collapse;"> <thead> <tr> <th>Angle</th> <th>Sin</th> <th>Cos</th> <th>Tan</th> </tr> </thead> <tbody> <tr> <td>0°</td> <td>0</td> <td>1</td> <td>0</td> </tr> <tr> <td>30°</td> <td>1/2</td> <td>$\sqrt{3}/2$</td> <td>$\sqrt{3}/3$</td> </tr> <tr> <td>37°</td> <td>3/5</td> <td>4/5</td> <td>3/4</td> </tr> <tr> <td>45°</td> <td>$\sqrt{2}/2$</td> <td>$\sqrt{2}/2$</td> <td>1</td> </tr> <tr> <td>53°</td> <td>4/5</td> <td>3/5</td> <td>4/3</td> </tr> <tr> <td>60°</td> <td>$\sqrt{3}/2$</td> <td>1/2</td> <td>$\sqrt{3}$</td> </tr> <tr> <td>90°</td> <td>1</td> <td>0</td> <td>∞</td> </tr> </tbody> </table>			Angle	Sin	Cos	Tan	0°	0	1	0	30°	1/2	$\sqrt{3}/2$	$\sqrt{3}/3$	37°	3/5	4/5	3/4	45°	$\sqrt{2}/2$	$\sqrt{2}/2$	1	53°	4/5	3/5	4/3	60°	$\sqrt{3}/2$	1/2	$\sqrt{3}$	90°	1	0	∞
Angle	Sin	Cos	Tan																																			
0°	0	1	0																																			
30°	1/2	$\sqrt{3}/2$	$\sqrt{3}/3$																																			
37°	3/5	4/5	3/4																																			
45°	$\sqrt{2}/2$	$\sqrt{2}/2$	1																																			
53°	4/5	3/5	4/3																																			
60°	$\sqrt{3}/2$	1/2	$\sqrt{3}$																																			
90°	1	0	∞																																			
	$hc = 1.99 \times 10^{-25} \text{ J} \cdot \text{m}$ $= 1.24 \times 10^3 \text{ eV} \cdot \text{nm}$	joule	J																																			
Vacuum permittivity,	$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{N} \cdot \text{m}^2$	watt	W																																			
Coulomb's law constant,	$k = 1/4\pi\epsilon_0 = 9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$	coulomb	C																																			
Vacuum permeability,	$\mu_0 = 4\pi \times 10^{-7} (\text{T} \cdot \text{m})/\text{A}$	volt	V																																			
Magnetic constant,	$k' = \mu_0/4\pi = 10^{-7} (\text{T} \cdot \text{m})/\text{A}$	ohm	Ω																																			
Universal gravitational constant,	$G = 6.67 \times 10^{-11} \text{ m}^3/\text{kg} \cdot \text{s}^2$	henry	H																																			
Acceleration due to gravity at the Earth's surface,	$g = 9.8 \text{ m/s}^2$	farad	F																																			
1 atmosphere pressure,	1 atm = $1.0 \times 10^5 \text{ N/m}^2$ $= 1.0 \times 10^5 \text{ Pa}$	tesla	T																																			
1 electron volt,	1 eV = $1.60 \times 10^{-19} \text{ J}$	degree Celsius	$^\circ\text{C}$																																			
1 angstrom,	1 Å = $1 \times 10^{-10} \text{ m}$	electron-volt	eV																																			

The following conventions are used in this examination.

- I. Unless otherwise stated, the frame of reference of any problem is assumed to be inertial.
- II. The direction of any electric current is the direction of flow of positive charge (conventional current).
- III. For any isolated electric charge, the electric potential is defined as zero at an infinite distance from the charge.

This insert may be used for reference and/or scratchwork as you answer the free-response questions, but be sure to show all your work and your answers in the pink booklet. No credit will be given for work shown on this green insert.

Copyright © 1998 by College Entrance Examination Board and Educational Testing Service.
All rights reserved.

For face-to-face teaching purposes, classroom teachers are permitted to reproduce only the questions in this green insert.

ADVANCED PLACEMENT PHYSICS C EQUATIONS FOR 1998

MECHANICS

$$v = v_0 + at$$

$$s = s_0 + v_0t + \frac{1}{2}at^2$$

$$v^2 = v_0^2 + 2a(s - s_0)$$

$$\Sigma \mathbf{F} = \mathbf{F}_{net} = ma$$

$$\mathbf{F} = \frac{d\mathbf{p}}{dt}$$

$$\mathbf{J} = \int \mathbf{F} \cdot dt = \Delta \mathbf{p}$$

$$\mathbf{p} = m\mathbf{v}$$

$$Ff \leq \mu N$$

$$W = \int \mathbf{F} \cdot ds$$

$$K = \frac{1}{2}mv^2$$

$$P = \frac{dW}{dt}$$

$$\Delta U_g = mgh$$

$$a_c = \frac{v^2}{r} = \omega^2 r$$

$$\boldsymbol{\tau} = \mathbf{r} \times \mathbf{F}$$

$$\Sigma \boldsymbol{\tau} = \boldsymbol{\tau}_{net} = I\boldsymbol{\alpha}$$

$$I = \int r^2 dm = \Sigma mr^2$$

$$r_{cm} = \Sigma m\mathbf{r} / \Sigma m$$

$$v = r\omega$$

$$\mathbf{L} = I\boldsymbol{\omega}$$

$$K = \frac{1}{2}I\omega^2$$

$$\omega = \omega_0 + \alpha t$$

$$\theta = \theta_0 + \omega_0 t + \frac{1}{2}\alpha t^2$$

$$\mathbf{F}_s = -k\mathbf{x}$$

$$U_s = \frac{1}{2}kx^2$$

$$T = \frac{2\pi}{\omega} = \frac{1}{f}$$

$$T_s = 2\pi\sqrt{\frac{m}{k}}$$

$$T_p = 2\pi\sqrt{\frac{\ell}{g}}$$

$$F_G = -\frac{Gm_1m_2}{r^2}$$

$$U_G = -\frac{Gm_1m_2}{r}$$

a = acceleration
 F = force
 f = frequency
 h = height
 I = rotational inertia
 J = impulse
 K = kinetic energy
 k = spring constant
 ℓ = length
 L = angular momentum
 m = mass
 N = normal force
 P = power
 p = momentum
 r = distance
 s = displacement
 T = period
 t = time
 U = potential energy
 v = velocity or speed
 W = work
 x = displacement
 μ = coefficient of friction
 θ = angle
 $\boldsymbol{\tau}$ = torque
 ω = angular speed
 $\boldsymbol{\alpha}$ = angular acceleration

ELECTRICITY AND MAGNETISM

$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1q_2}{r^2}$$

$$\mathbf{E} = \frac{\mathbf{F}}{q}$$

$$\int \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$$

$$E = \frac{dV}{dr}$$

$$V = \frac{1}{4\pi\epsilon_0} \Sigma \frac{q}{r}$$

$$U_E = qV = F = \frac{1}{4\pi\epsilon_0} \frac{q_1q_2}{r^2}$$

$$C = \frac{Q}{V}$$

$$C = \frac{\kappa\epsilon_0 A}{d}$$

$$C_p = \Sigma_i C_i$$

$$\frac{1}{C_s} = \Sigma_i \frac{1}{C_i}$$

$$I = \frac{dQ}{dt}$$

$$U_c = \frac{1}{2}QV = \frac{1}{2}CV^2$$

$$R = \frac{\rho\ell}{A}$$

$$V = IR$$

$$R_s = \Sigma_i R_i$$

$$\frac{1}{R_p} = \Sigma_i \frac{1}{R_i}$$

$$P = IV$$

$$\mathbf{F}_M = q\mathbf{v} \times \mathbf{B}$$

$$\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 I$$

$$\mathbf{F} = \int I d\mathbf{l} \times \mathbf{B}$$

$$B_s = \mu_0 nI$$

$$\phi_m = \int \mathbf{B} \cdot d\mathbf{A}$$

$$\mathcal{E} = -\frac{d\phi_m}{dt}$$

$$\mathcal{E} = -L \frac{dI}{dt}$$

$$U_L = \frac{1}{2}LI^2$$

A = area
 B = magnetic field strength
 C = capacitance
 d = distance
 E = electric field strength
 \mathcal{E} = emf
 F = force
 I = current
 L = inductance
 ℓ = length
 n = number of loops of wire per unit length
 P = power
 Q = charge
 q = point charge
 R = resistance
 r = distance
 t = time
 U = potential or stored energy
 V = electric potential
 v = velocity or speed
 ρ = resistivity
 ϕ_m = magnetic flux
 κ = dielectric constant

GEOMETRY AND TRIGONOMETRY

Rectangle

$$A = bh$$

Triangle

$$A = \frac{1}{2}bh$$

Circle

$$A = \pi r^2$$

$$C = 2\pi r$$

Parallelepiped

$$V = \ell wh$$

Cylinder

$$V = \pi r^2 \ell$$

$$S = 2\pi r \ell + 2\pi r^2$$

Sphere

$$V = \frac{4}{3}\pi r^3$$

$$S = 4\pi r^2$$

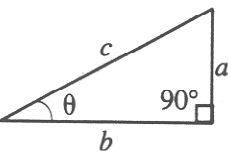
Right Triangle

$$a^2 + b^2 = c^2$$

$$\sin \theta = \frac{a}{c}$$

$$\cos \theta = \frac{b}{c}$$

$$\tan \theta = \frac{a}{b}$$



A = area
 C = circumference
 V = volume
 S = surface area
 b = base
 h = height
 ℓ = length
 w = width
 r = radius

CALCULUS

$$\frac{df}{dx} = \frac{df}{du} \cdot \frac{du}{dx}$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\ln x) = \frac{1}{x}$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\int x^n dx = \frac{1}{n+1} x^{n+1}, n \neq -1$$

$$\int e^x dx = e^x$$

$$\int \frac{dx}{x} = \ln|x|$$

$$\int \cos x dx = \sin x$$

$$\int \sin x dx = -\cos x$$

Attention AP Physics C Candidates

This sheet of equations replaces pages 2 and 3 (unnumbered) in the green insert of the pink Section II exam booklet.

ADVANCED PLACEMENT PHYSICS C EQUATIONS FOR 1998

MECHANICS

$v = v_0 + at$ $s = s_0 + v_0 t + \frac{1}{2} at^2$ $v^2 = v_0^2 + 2a(s - s_0)$ $\Sigma \mathbf{F} = \mathbf{F}_{net} = m\mathbf{a}$ $\mathbf{F} = \frac{d\mathbf{p}}{dt}$ $\mathbf{J} = \int \mathbf{F} dt = \Delta \mathbf{p}$ $\mathbf{p} = m\mathbf{v}$ $F_{fric} \leq \mu N$ $W = \int \mathbf{F} \cdot d\mathbf{s}$ $K = \frac{1}{2} m v^2$ $P = \frac{dW}{dt}$ $\Delta U_g = mgh$ $a_c = \frac{v^2}{r} = \omega^2 r$ $\boldsymbol{\tau} = \mathbf{r} \times \mathbf{F}$ $\Sigma \boldsymbol{\tau} = \boldsymbol{\tau}_{net} = I\boldsymbol{\alpha}$ $I = \int r^2 dm = \Sigma mr^2$ $\mathbf{r}_{cm} = \Sigma m\mathbf{r} / \Sigma m$ $v = r\omega$ $\mathbf{L} = \mathbf{r} \times \mathbf{p} = I\boldsymbol{\omega}$ $K = \frac{1}{2} I\omega^2$ $\omega = \omega_0 + \alpha t$ $\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2$ $\mathbf{F}_s = -k\mathbf{x}$ $U_s = \frac{1}{2} kx^2$ $T = \frac{2\pi}{\omega} = \frac{1}{f}$ $T_s = 2\pi \sqrt{\frac{m}{k}}$ $T_p = 2\pi \sqrt{\frac{\ell}{g}}$ $F_G = -\frac{Gm_1 m_2}{r^2}$ $U_G = -\frac{Gm_1 m_2}{r}$	<p><i>a</i> = acceleration <i>F</i> = force <i>f</i> = frequency <i>h</i> = height <i>I</i> = rotational inertia <i>J</i> = impulse <i>K</i> = kinetic energy <i>k</i> = spring constant <i>ℓ</i> = length <i>L</i> = angular momentum <i>m</i> = mass <i>N</i> = normal force <i>P</i> = power <i>p</i> = momentum <i>r</i> = distance <i>s</i> = displacement <i>T</i> = period <i>t</i> = time <i>U</i> = potential energy <i>v</i> = velocity or speed <i>W</i> = work <i>x</i> = displacement <i>μ</i> = coefficient of friction <i>θ</i> = angle <i>τ</i> = torque <i>ω</i> = angular speed <i>α</i> = angular acceleration</p>
--	---

ELECTRICITY AND MAGNETISM

$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$ $\mathbf{E} = \frac{\mathbf{F}}{q}$ $\oint \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$ $E = -\frac{dV}{dr}$ $V = \frac{1}{4\pi\epsilon_0} \sum \frac{q}{r}$ $U_E = qV = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r}$ $C = \frac{Q}{V}$ $C = \frac{\kappa\epsilon_0 A}{d}$ $C_p = \sum_i C_i$ $\frac{1}{C_s} = \sum_i \frac{1}{C_i}$ $I = \frac{dQ}{dt}$ $U_c = \frac{1}{2} QV = \frac{1}{2} CV^2$ $R = \frac{\rho \ell}{A}$ $V = IR$ $R_s = \sum_i R_i$ $\frac{1}{R_p} = \sum_i \frac{1}{R_i}$ $P = IV$ $\mathbf{F}_M = q\mathbf{v} \times \mathbf{B}$ $\oint \mathbf{B} \cdot d\boldsymbol{\ell} = \mu_0 I$ $\mathbf{F} = \int I d\boldsymbol{\ell} \times \mathbf{B}$ $B_s = \mu_0 nI$ $\Phi_m = \int \mathbf{B} \cdot d\mathbf{A}$ $\mathcal{E} = -\frac{d\Phi_m}{dt}$ $\mathcal{E} = -L \frac{dI}{dt}$ $U_L = \frac{1}{2} LI^2$	<p><i>A</i> = area <i>B</i> = magnetic field <i>C</i> = capacitance <i>d</i> = distance <i>E</i> = electric field <i>ℰ</i> = emf <i>F</i> = force <i>I</i> = current <i>L</i> = inductance <i>ℓ</i> = length <i>n</i> = number of loops of wire per unit length <i>P</i> = power <i>Q</i> = charge <i>q</i> = point charge <i>R</i> = resistance <i>r</i> = distance <i>t</i> = time <i>U</i> = potential or stored energy <i>V</i> = electric potential <i>v</i> = velocity or speed <i>ρ</i> = resistivity <i>Φ_m</i> = magnetic flux <i>κ</i> = dielectric constant</p>
--	--

GEOMETRY AND TRIGONOMETRY

Rectangle

$$A = bh$$

Triangle

$$A = \frac{1}{2}bh$$

Circle

$$A = \pi r^2$$

$$C = 2\pi r$$

Parallelepiped

$$V = \ell wh$$

Cylinder

$$V = \pi r^2 \ell$$

$$S = 2\pi r \ell + 2\pi r^2$$

Sphere

$$V = \frac{4}{3}\pi r^3$$

$$S = 4\pi r^2$$

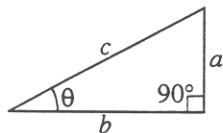
Right Triangle

$$a^2 + b^2 = c^2$$

$$\sin \theta = \frac{a}{c}$$

$$\cos \theta = \frac{b}{c}$$

$$\tan \theta = \frac{a}{b}$$

 $A = \text{area}$
 $C = \text{circumference}$
 $V = \text{volume}$
 $S = \text{surface area}$
 $b = \text{base}$
 $h = \text{height}$
 $\ell = \text{length}$
 $w = \text{width}$
 $r = \text{radius}$

CALCULUS

$$\frac{df}{dx} = \frac{df}{du} \cdot \frac{du}{dx}$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(\ln x) = \frac{1}{x}$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\int x^n dx = \frac{1}{n+1} x^{n+1}, n \neq -1$$

$$\int e^x dx = e^x$$

$$\int \frac{dx}{x} = \ln |x|$$

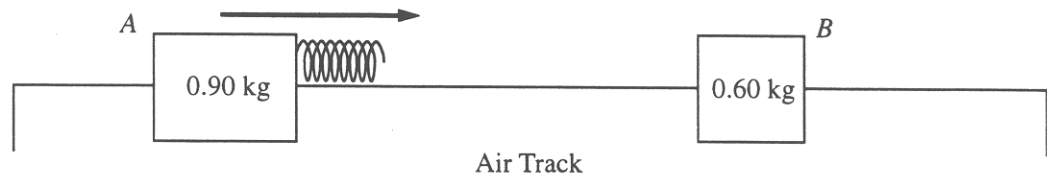
$$\int \cos x dx = \sin x$$

$$\int \sin x dx = -\cos x$$

PHYSICS C
SECTION II, MECHANICS

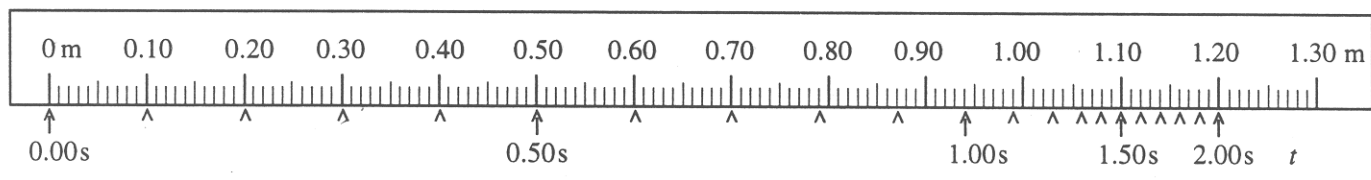
Time—45 minutes
3 Questions

Directions: Answer all three questions. The suggested time is about 15 minutes for answering each of the questions, which are worth 15 points each. The parts within a question may not have equal weight. Show all your work in the pink booklet in the spaces provided after each part, NOT in this green insert.



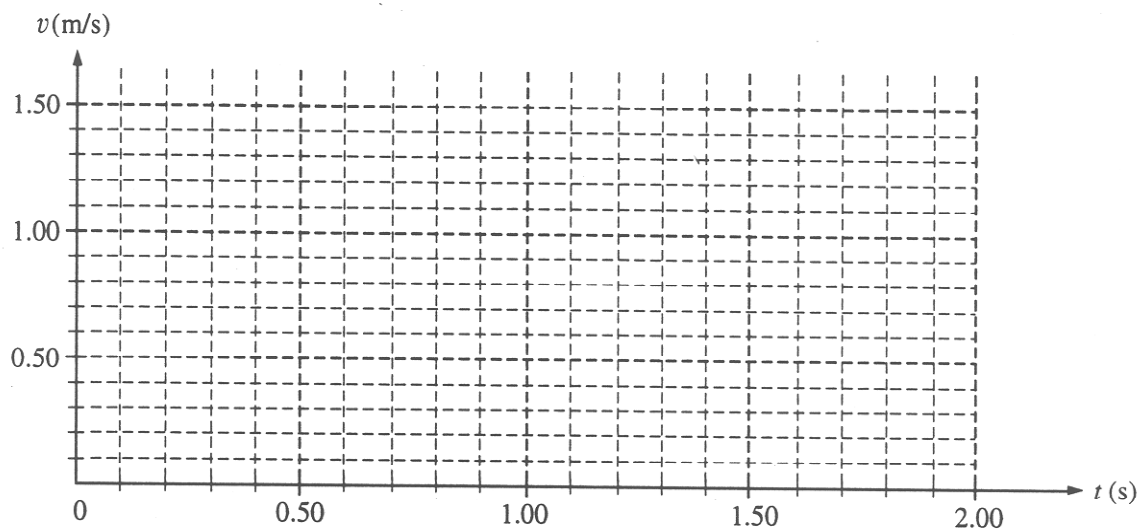
Mech. 1. Two gliders move freely on an air track with negligible friction, as shown above. Glider *A* has a mass of 0.90 kg and glider *B* has a mass of 0.60 kg. Initially, glider *A* moves toward glider *B*, which is at rest. A spring of negligible mass is attached to the right side of glider *A*. Strobe photography is used to record successive positions of glider *A* at 0.10 s intervals over a total time of 2.00 s, during which time it collides with glider *B*.

The following diagram represents the data for the motion of glider *A*. Positions of glider *A* at the end of each 0.10 s interval are indicated by the symbol \wedge against a metric ruler. The total elapsed time t after each 0.50 s is also indicated.



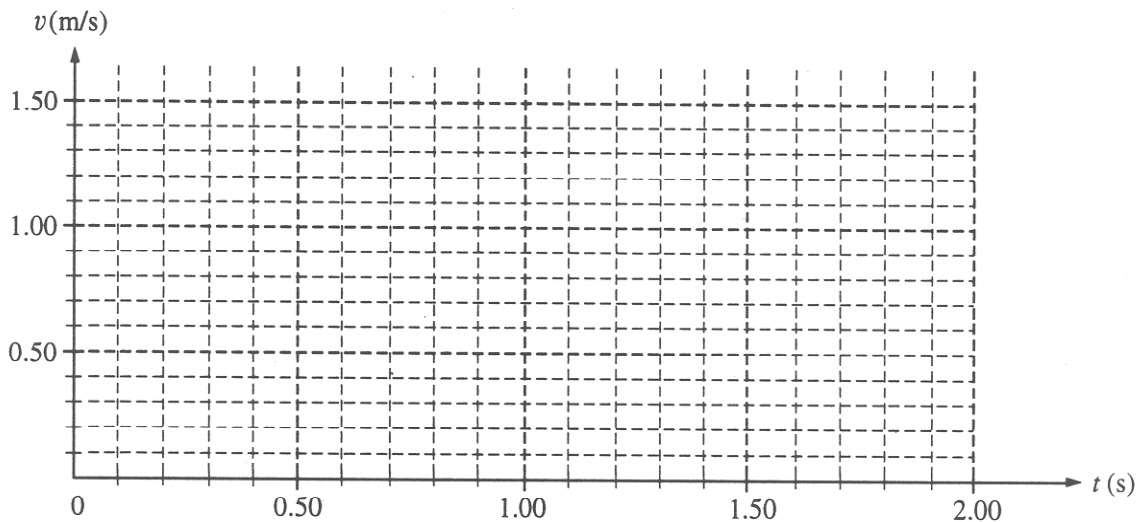
- (a) Determine the average speed of glider *A* for the following time intervals.
- i. 0.10 s to 0.30 s
 - ii. 0.90 s to 1.10 s
 - iii. 1.70 s to 1.90 s

(b) On the axes below, sketch a graph, consistent with the data above, of the speed of glider *A* as a function of time *t* for the 2.00 s interval.



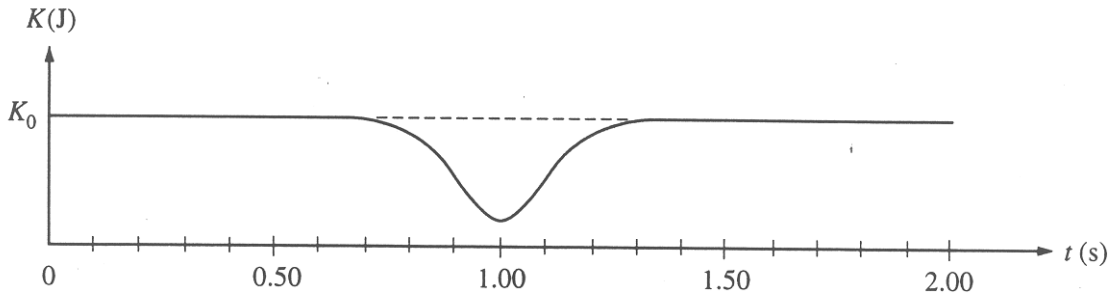
(c) i. Use the data to calculate the speed of glider *B* immediately after it separates from the spring.

ii. On the axes below, sketch a graph of the speed of glider *B* as a function of time *t*.



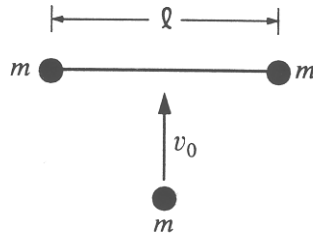
GO ON TO THE NEXT PAGE

A graph of the total kinetic energy K for the two-glider system over the 2.00 s interval has the following shape. K_0 is the total kinetic energy of the system at time $t = 0$.

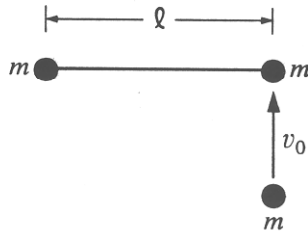


- (d) i. Is the collision elastic? Justify your answer.
- ii. Briefly explain why there is a minimum in the kinetic energy curve at $t = 1.00$ s.

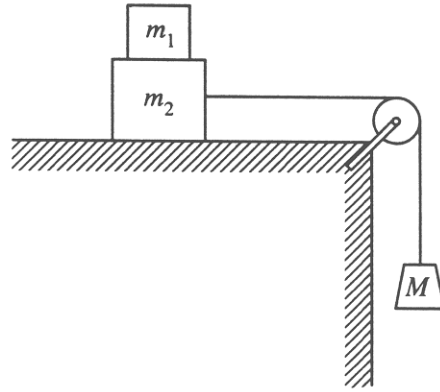
Mech. 2. A space shuttle astronaut in a circular orbit around the Earth has an assembly consisting of two small dense spheres, each of mass m , whose centers are connected by a rigid rod of length ℓ and negligible mass. The astronaut also has a device that will launch a small lump of clay of mass m at speed v_0 . Express your answers in terms of m , v_0 , ℓ , and fundamental constants.



- (a) Initially, the assembly is “floating” freely at rest relative to the cabin, and the astronaut launches the clay lump so that it perpendicularly strikes and sticks to the midpoint of the rod, as shown above.
- i. Determine the total kinetic energy of the system (assembly and clay lump) after the collision.
 - ii. Determine the change in kinetic energy as a result of the collision.



- (b) The assembly is brought to rest, the clay lump removed, and the experiment is repeated as shown above, with the clay lump striking perpendicular to the rod but this time sticking to one of the spheres of the assembly.
- i. Determine the distance from the left end of the rod to the center of mass of the system (assembly and clay lump) immediately after the collision. (Assume that the radii of the spheres and clay lump are much smaller than the separation of the spheres.)
 - ii. On the figure above, indicate the direction of the motion of the center of mass immediately after the collision.
 - iii. Determine the speed of the center of mass immediately after the collision.
 - iv. Determine the angular speed of the system (assembly and clay lump) immediately after the collision.
 - v. Determine the change in kinetic energy as a result of the collision.



Mech. 3. Block 1 of mass m_1 is placed on block 2 of mass m_2 , which is then placed on a table. A string connecting block 2 to a hanging mass M passes over a pulley attached to one end of the table, as shown above. The mass and friction of the pulley are negligible. The coefficients of friction between blocks 1 and 2 and between block 2 and the tabletop are nonzero and are given in the following table.

	Coefficient Between Blocks 1 and 2	Coefficient Between Block 2 and the Tabletop
Static	μ_{s1}	μ_{s2}
Kinetic	μ_{k1}	μ_{k2}

Express your answers in terms of the masses, coefficients of friction, and g , the acceleration due to gravity.

(a) Suppose that the value of M is small enough that the blocks remain at rest when released. For each of the following forces, determine the magnitude of the force and draw a vector on the block provided to indicate the direction of the force if it is nonzero.

i. The normal force N_1 exerted on block 1 by block 2



ii. The friction force f_1 exerted on block 1 by block 2



iii. The force T exerted on block 2 by the string



iv. The normal force N_2 exerted on block 2 by the tabletop



v. The friction force f_2 exerted on block 2 by the tabletop



- (b) Determine the largest value of M for which the blocks can remain at rest.
- (c) Now suppose that M is large enough that the hanging block descends when the blocks are released. Assume that blocks 1 and 2 are moving as a unit (no slippage). Determine the magnitude a of their acceleration.
- (d) Now suppose that M is large enough that as the hanging block descends, block 1 is slipping on block 2. Determine each of the following.
 - i. The magnitude a_1 of the acceleration of block 1
 - ii. The magnitude a_2 of the acceleration of block 2

STOP

END OF SECTION II, MECHANICS

IF YOU FINISH BEFORE TIME IS CALLED, YOU MAY CHECK YOUR WORK ON SECTION II, MECHANICS, ONLY. DO NOT TURN TO ANY OTHER TEST MATERIALS.

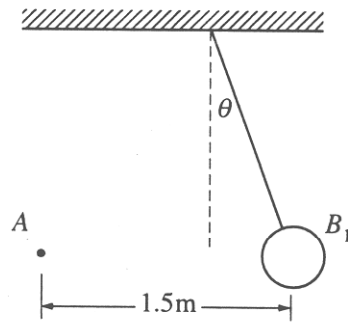
NO TEST MATERIAL ON THIS PAGE

PHYSICS C
SECTION II, ELECTRICITY AND MAGNETISM

Time—45 minutes

3 Questions

Directions: Answer all three questions. The suggested time is about 15 minutes for answering each of the questions, which are worth 15 points each. The parts within a question may not have equal weight. Show all your work in the pink booklet in the spaces provided after each part, NOT in this green insert.



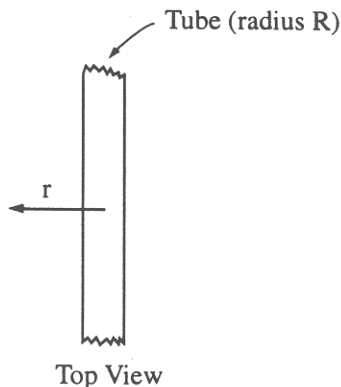
Note: Figure not drawn to scale.

E & M. 1. The small sphere A in the diagram above has a charge of $120 \mu\text{C}$. The large sphere B_1 is a thin shell of nonconducting material with a net charge that is uniformly distributed over its surface. Sphere B_1 has a mass of 0.025 kg , a radius of 0.05 m , and is suspended from an uncharged, nonconducting thread. Sphere B_1 is in equilibrium when the thread makes an angle $\theta = 20^\circ$ with the vertical. The centers of the spheres are at the same vertical height and are a horizontal distance of 1.5 m apart, as shown.

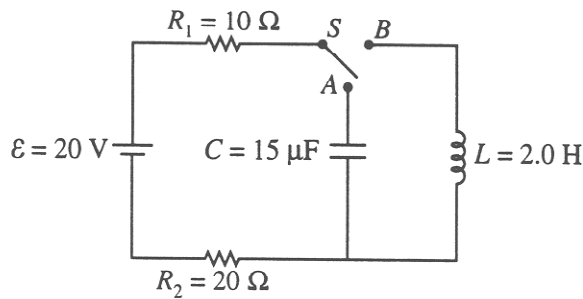
- (a) Calculate the charge on sphere B_1 .
- (b) Suppose that sphere B_1 is replaced by a second suspended sphere B_2 that has the same mass, radius, and charge, but that is conducting. Equilibrium is again established when sphere A is 1.5 m from sphere B_2 and their centers are at the same vertical height. State whether the equilibrium angle θ_2 will be less than, equal to, or greater than 20° . Justify your answer.

E E E E E E E E E E E E E E E E E E E

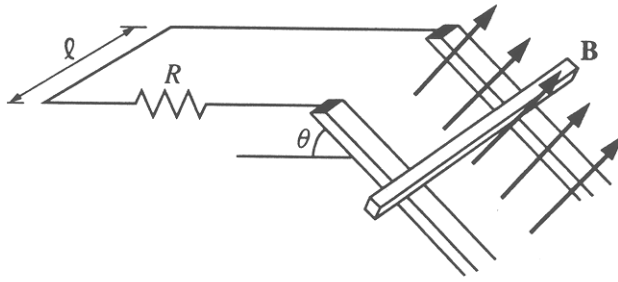
The sphere B_2 is now replaced by a very long, horizontal, nonconducting tube, as shown in the top view below. The tube is hollow with thin walls of radius $R = 0.20$ m and a uniform positive charge per unit length of $\lambda = +0.10 \mu\text{C}/\text{m}$.



- (c) Use Gauss's law to show that the electric field at a perpendicular distance r from the tube is given by the expression $E = \frac{1.8 \times 10^3}{r}$ N/C, where $r > R$ and r is in meters.
- (d) The small sphere A with charge $120 \mu\text{C}$ is now brought into the vicinity of the tube and is held at a distance of $r = 1.5$ m from the center of the tube. Calculate the repulsive force that the tube exerts on the sphere.
- (e) Calculate the work done against the electrostatic repulsion to move sphere A toward the tube from a distance $r = 1.5$ m to a distance $r = 0.3$ m from the tube.



- E & M. 2. In the circuit shown above, the switch S is initially in the open position shown, and the capacitor is uncharged. A voltmeter (not shown) is used to measure the correct potential difference across resistor R_1 .
- On the circuit diagram above, draw the voltmeter with the proper connections for correctly measuring the potential difference across resistor R_1 .
 - At time $t = 0$, the switch is moved to position A . Determine the voltmeter reading for the time immediately after $t = 0$.
 - After a long time, a measurement of potential difference across R_1 is again taken. Determine for this later time each of the following.
 - The voltmeter reading
 - The charge on the capacitor
 - At a still later time $t = T$, the switch S is moved to position B . Determine the voltmeter reading for the time immediately after $t = T$.
 - A long time after $t = T$, the current in R_1 reaches a constant final value I_f .
 - Determine I_f .
 - Determine the final energy stored in the inductor.
 - Write, but do not solve, a differential equation for the current in resistor R_1 as a function of time t after the switch is moved to position B .



E & M. 3. A conducting bar of mass m is placed on two long conducting rails a distance l apart. The rails are inclined at an angle θ with respect to the horizontal, as shown above, and the bar is able to slide on the rails with negligible friction. The bar and rails are in a uniform and constant magnetic field of magnitude B oriented perpendicular to the incline. A resistor of resistance R connects the upper ends of the rails and completes the circuit as shown. The bar is released from rest at the top of the incline. Express your answers to parts (a) through (d) in terms of m , l , θ , B , R , and g .

- Determine the current in the circuit when the bar has reached a constant final speed.
- Determine the constant final speed of the bar.
- Determine the rate at which energy is being dissipated in the circuit when the bar has reached its constant final speed.
- Express the speed of the bar as a function of time t from the time it is released at $t = 0$.
- Suppose that the experiment is performed again, this time with a second identical resistor connecting the rails at the bottom of the incline. Will this affect the final speed attained by the bar, and if so, how? Justify your answer.

S T O P

END OF SECTION II, ELECTRICITY AND MAGNETISM

IF YOU FINISH BEFORE TIME IS CALLED, YOU MAY CHECK YOUR WORK ON SECTION II, ELECTRICITY AND MAGNETISM, ONLY. DO NOT TURN TO ANY OTHER TEST MATERIALS.

NO TEST MATERIAL ON THIS PAGE

